

G5BAIM

Artificial Intelligence Methods

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Neural Networks



Neural Networks

- **AIMA – Chapter 19**
- **Fundamentals of Neural Networks : Architectures, Algorithms and Applications. L, Fausett, 1994**
- **An Introduction to Neural Networks (2nd Ed). Morton, IM, 1995**

Neural Networks

- **McCulloch & Pitts (1943) are generally recognised as the designers of the first neural network**
- **Many of their ideas still used today (e.g. many simple units combine to give increased computational power and the idea of a threshold)**

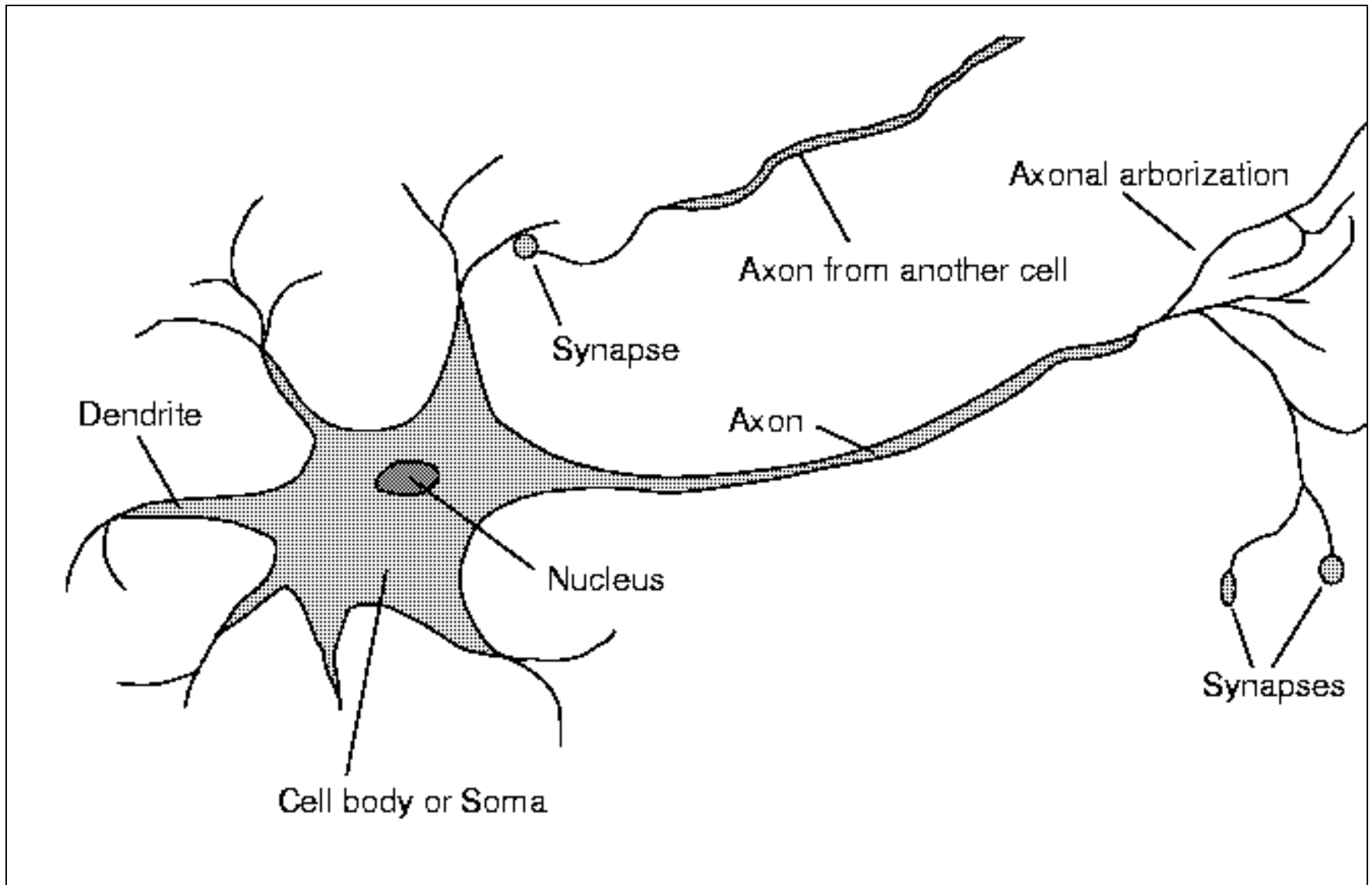
Neural Networks

- **Hebb (1949) developed the first learning rule (on the premise that if two neurons were active at the same time the strength between them should be increased)**

Neural Networks

- **During the 50's and 60's many researchers worked on the perceptron amidst great excitement.**
- **1969 saw the death of neural network research for about 15 years – Minsky & Papert**
- **Only in the mid 80's (Parker and LeCun) was interest revived (in fact Werbos discovered algorithm in 1974)**

Neural Networks



Neural Networks

- **We are born with about 100 billion neurons**
- **A neuron may connect to as many as 100,000 other neurons**

Neural Networks

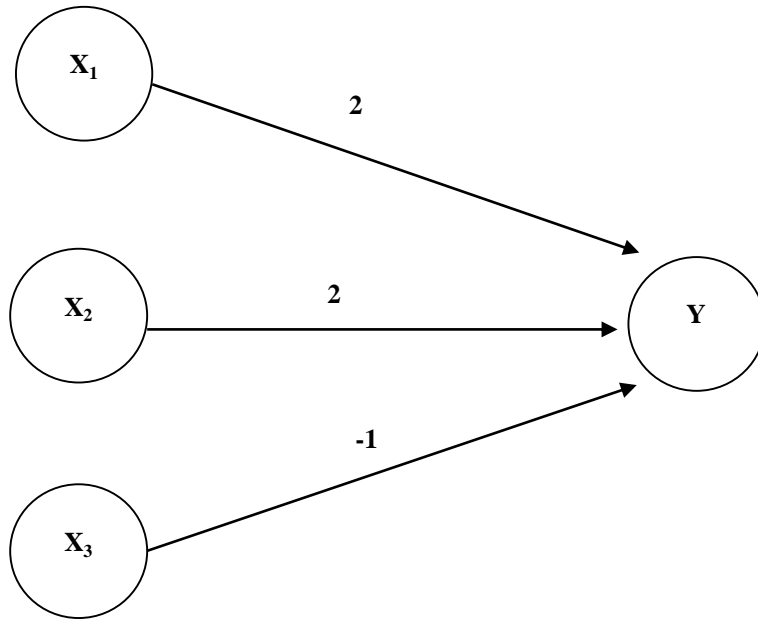
- **Signals “move” via electrochemical signals**
- **The synapses release a chemical transmitter – the sum of which can cause a threshold to be reached – causing the neuron to “fire”**
- **Synapses can be inhibitory or excitatory**

The First Neural Neural Networks

McCulloch and Pitts produced the first neural network in 1943

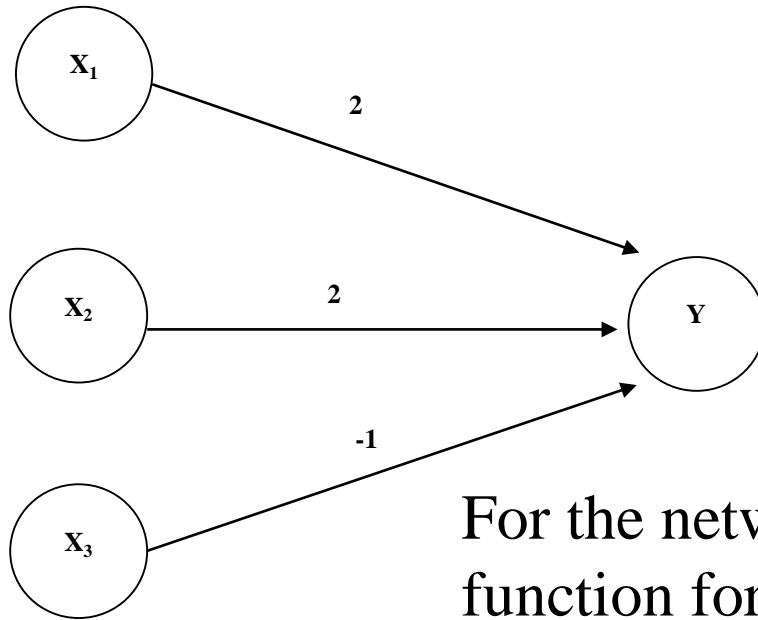
Many of the principles can still be seen in neural networks of today

The First Neural Neural Networks



The activation of a neuron is binary. That is, the neuron either fires (activation of one) or does not fire (activation of zero).

The First Neural Neural Networks

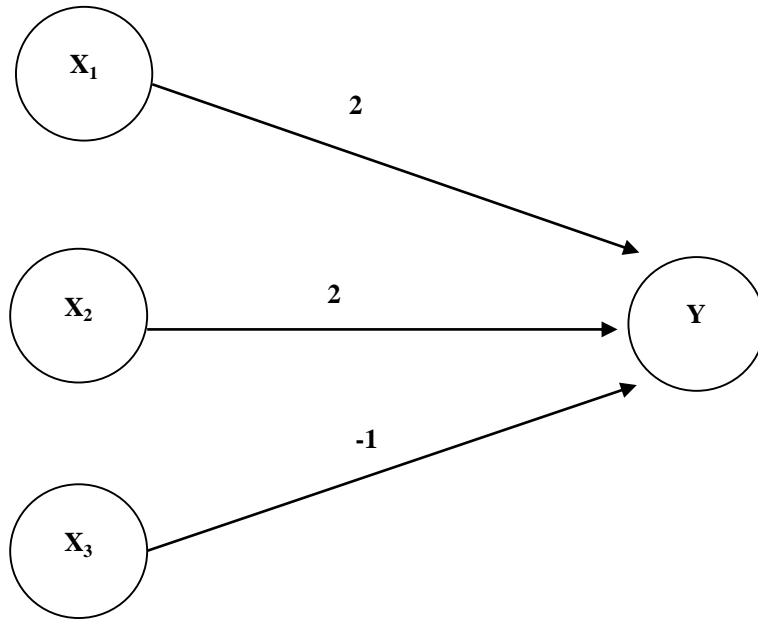


For the network shown here the activation function for unit Y is

$$f(y_{in}) = 1, \text{ if } y_{in} \geq \theta \text{ else } 0$$

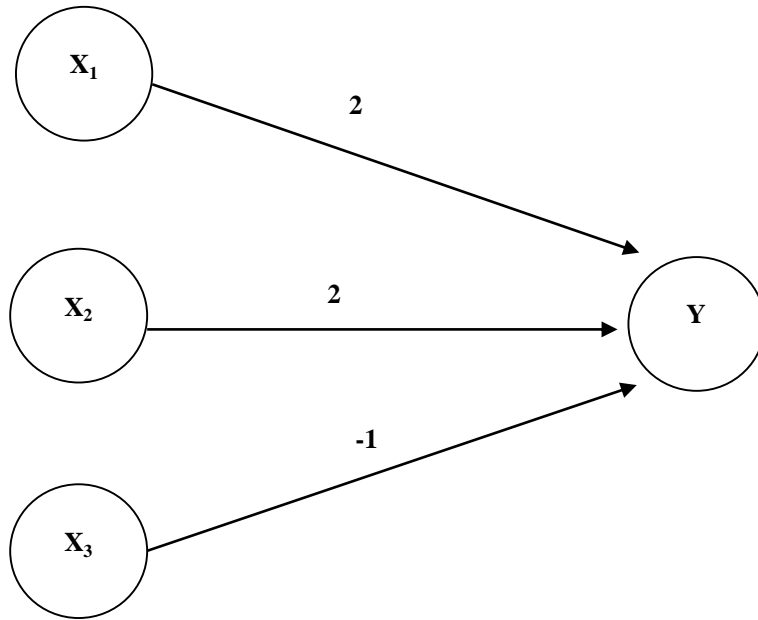
where y_{in} is the total input signal received
 θ is the threshold for Y

The First Neural Networks



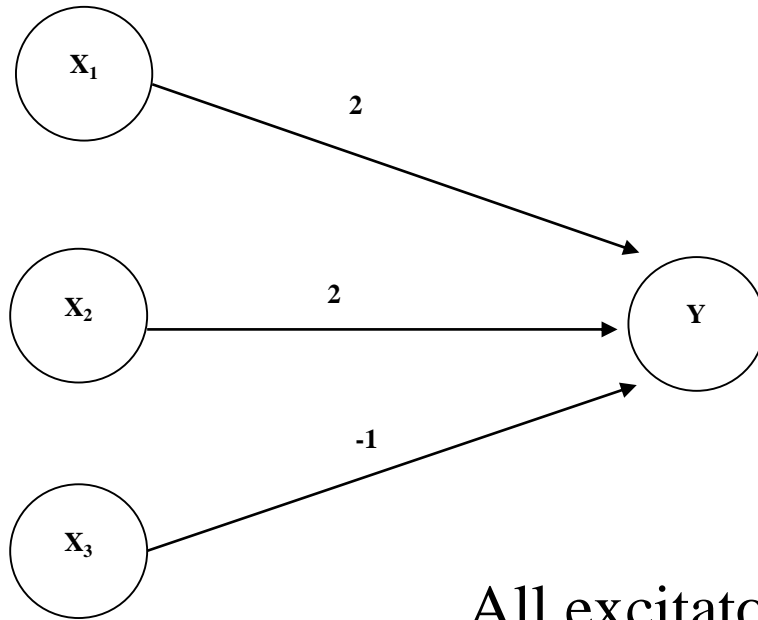
Neurons in a McCulloch-Pitts network are connected by directed, weighted paths

The First Neural Neural Networks



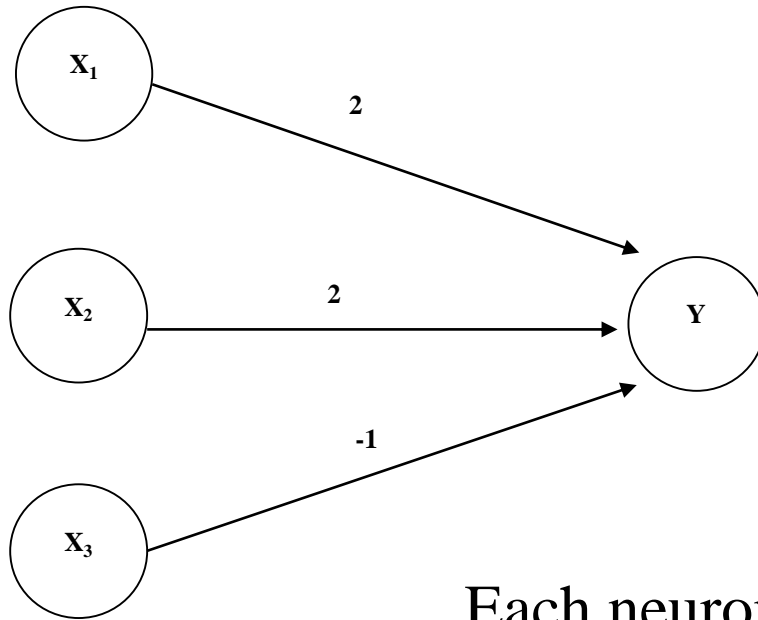
If the weight on a path is positive the path is excitatory, otherwise it is inhibitory

The First Neural Neural Networks



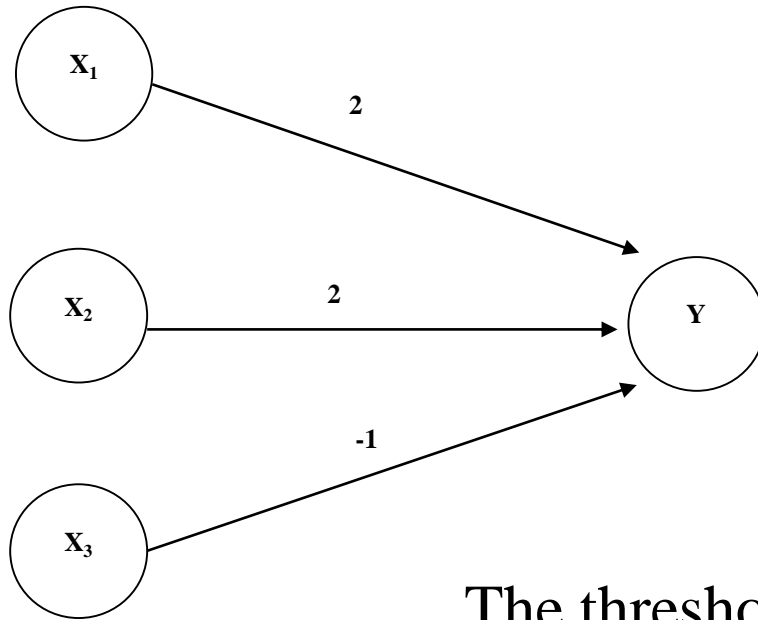
All excitatory connections into a particular neuron have the same weight, although different weighted connections can be input to different neurons

The First Neural Neural Networks



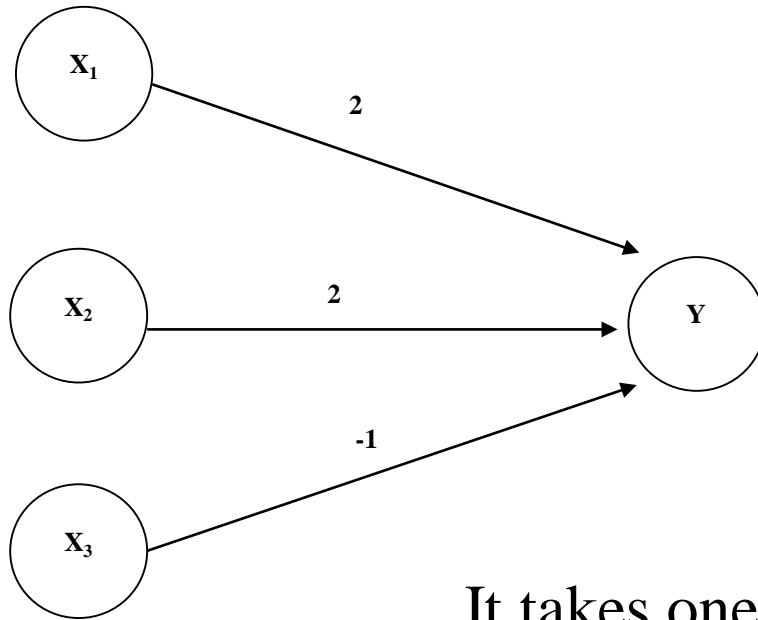
Each neuron has a fixed threshold. If the net input into the neuron is greater than the threshold, the neuron fires

The First Neural Neural Networks



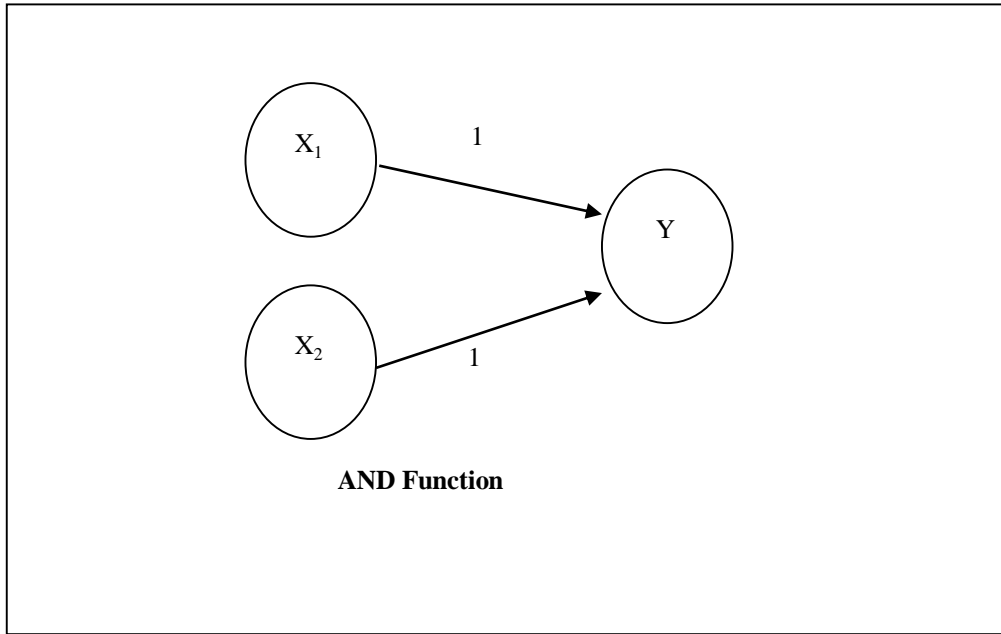
The threshold is set such that any non-zero inhibitory input will prevent the neuron from firing

The First Neural Neural Networks



It takes one time step for a signal to pass over one connection.

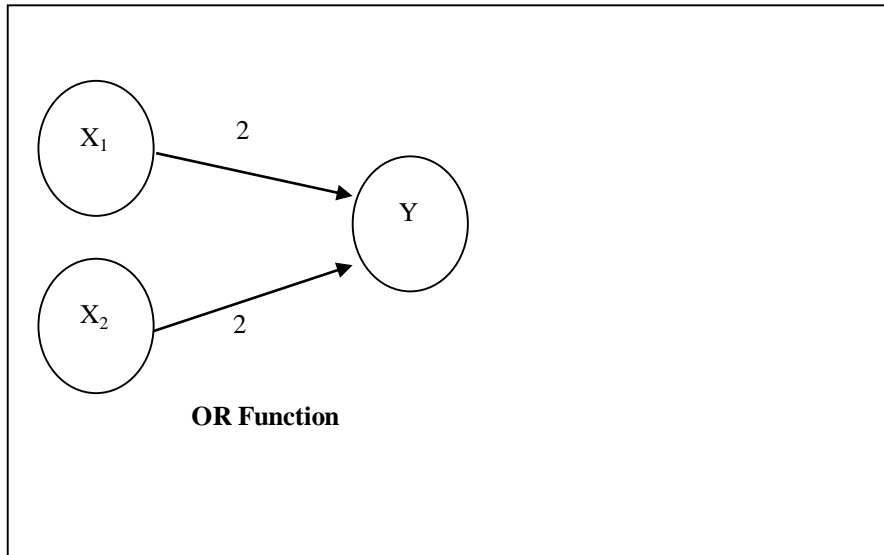
The First Neural Neural Networks



Threshold(Y) = 2

AND		
X1	X2	Y
1	1	1
1	0	0
0	1	0
0	0	0

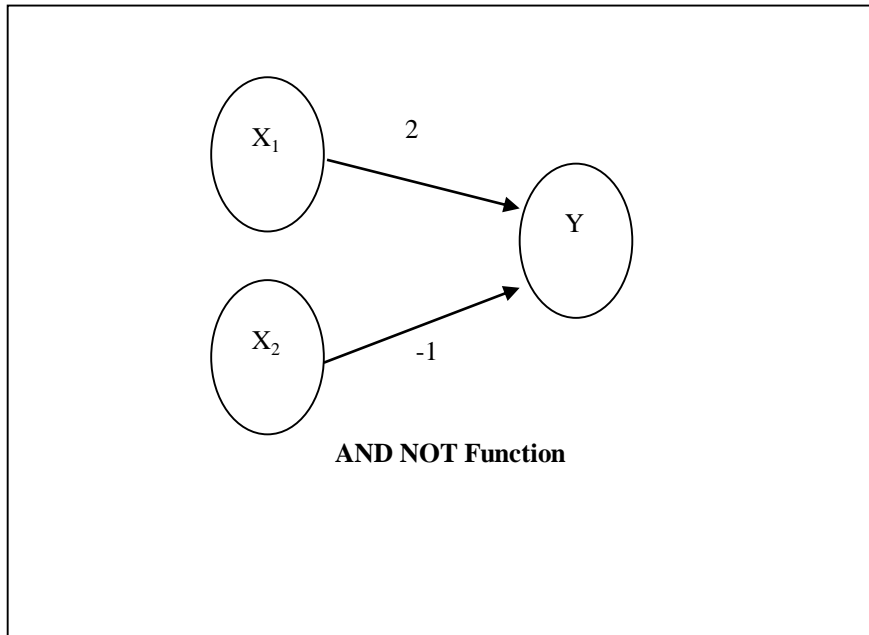
The First Neural Neural Networks



Threshold(Y) = 2

OR		
X1	X2	Y
1	1	1
1	0	1
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0	0	0

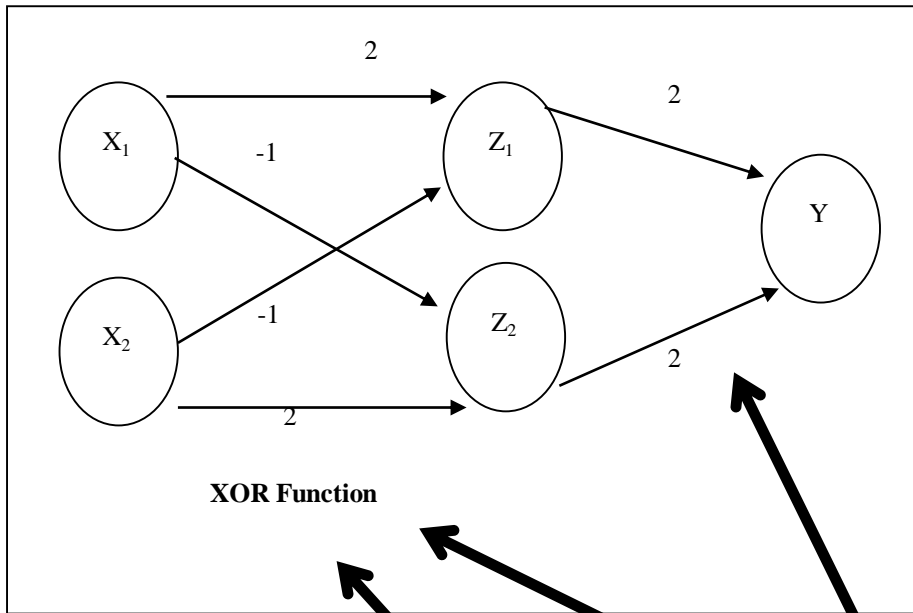
The First Neural Neural Networks



Threshold(Y) = 2

AND NOT		
X1	X2	Y
1	1	0
1	0	1
0	1	0
0	0	0

The First Neural Networks



XOR		
X1	X2	Y
1	1	0
1	0	1
0	1	1
0	0	0

$$X_1 \text{ XOR } X_2 = (X_1 \text{ AND NOT } X_2) \text{ OR } (X_2 \text{ AND NOT } X_1)$$

The First Neural Neural Networks

If we touch something cold we perceive heat

If we keep touching something cold we will perceive cold

If we touch something hot we will perceive heat

The First Neural Neural Networks

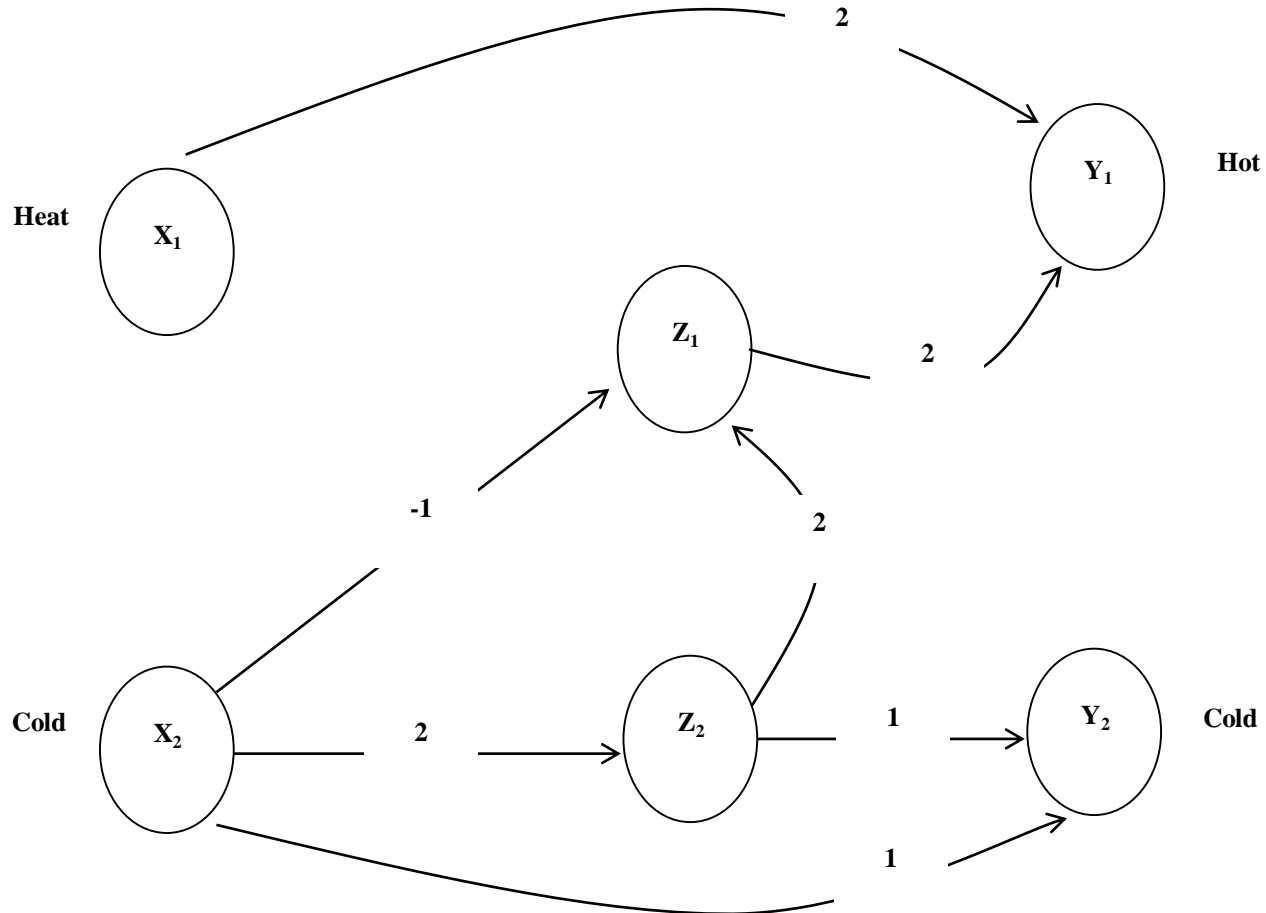
To model this we will assume that time is discrete

If cold is applied for one time step then heat will be perceived

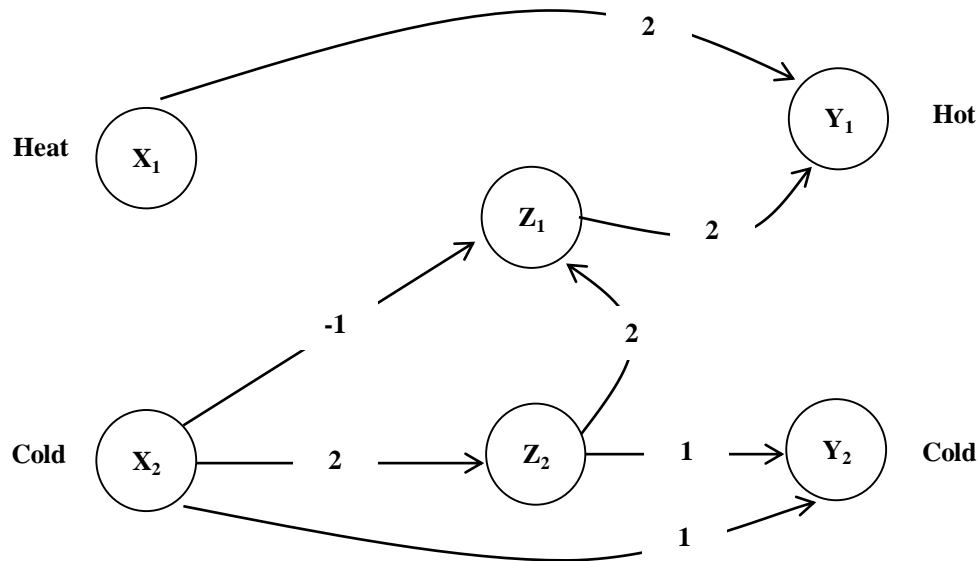
If a cold stimulus is applied for two time steps then cold will be perceived

If heat is applied then we should perceive heat

The First Neural Networks



The First Neural Neural Networks



- It takes time for the stimulus (applied at X_1 and X_2) to make its way to Y_1 and Y_2 where we perceive either heat or cold

- At $t(0)$, we apply a stimulus to X_1 and X_2
- At $t(1)$ we can update Z_1 , Z_2 and Y_1
- At $t(2)$ we can perceive a stimulus at Y_2
- At $t(2+n)$ the network is fully functional

The First Neural Neural Networks

We want the system to perceive cold if a cold stimulus is applied for two time steps

$$Y_2(t) = X_2(t - 2) \text{ AND } X_2(t - 1)$$

$X_2(t - 2)$	$X_2(t - 1)$	$Y_2(t)$
1	1	1
1	0	0
0	1	0
0	0	0

The First Neural Neural Networks

We want the system to perceive heat if either a hot stimulus is applied or a cold stimulus is applied (for one time step) and then removed

$$Y_1(t) = [X_1(t-1)] \text{ OR } [X_2(t-3) \text{ AND NOT } X_2(t-2)]$$

X2(t - 3)	X2(t - 2)	AND NOT	X1(t - 1)	OR
1	1	0	1	1
1	0	1	1	1
0	1	0	1	1
0	0	0	1	1
1	1	0	0	0
1	0	1	0	1
0	1	0	0	0
0	0	0	0	0

The First Neural Neural Networks

The network shows

$$Y_1(t) = X_1(t-1) \text{ OR } Z_1(t-1)$$

$$Z_1(t-1) = Z_2(t-2) \text{ AND NOT } X_2(t-2)$$

$$Z_2(t-2) = X_2(t-3)$$

Substituting, we get

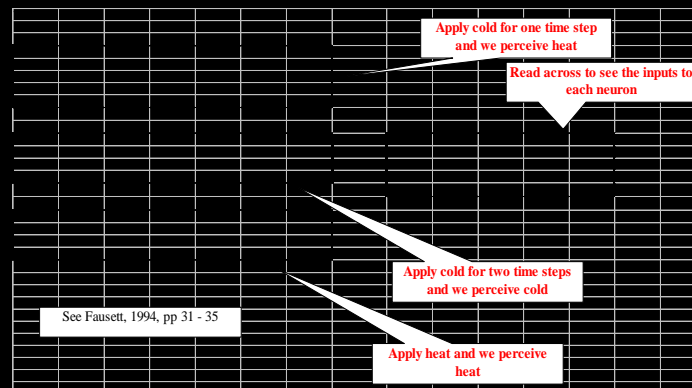
$$Y_1(t) = [X_1(t-1)] \text{ OR } [X_2(t-3) \text{ AND NOT } X_2(t-2)]$$

which is the same as our original requirements

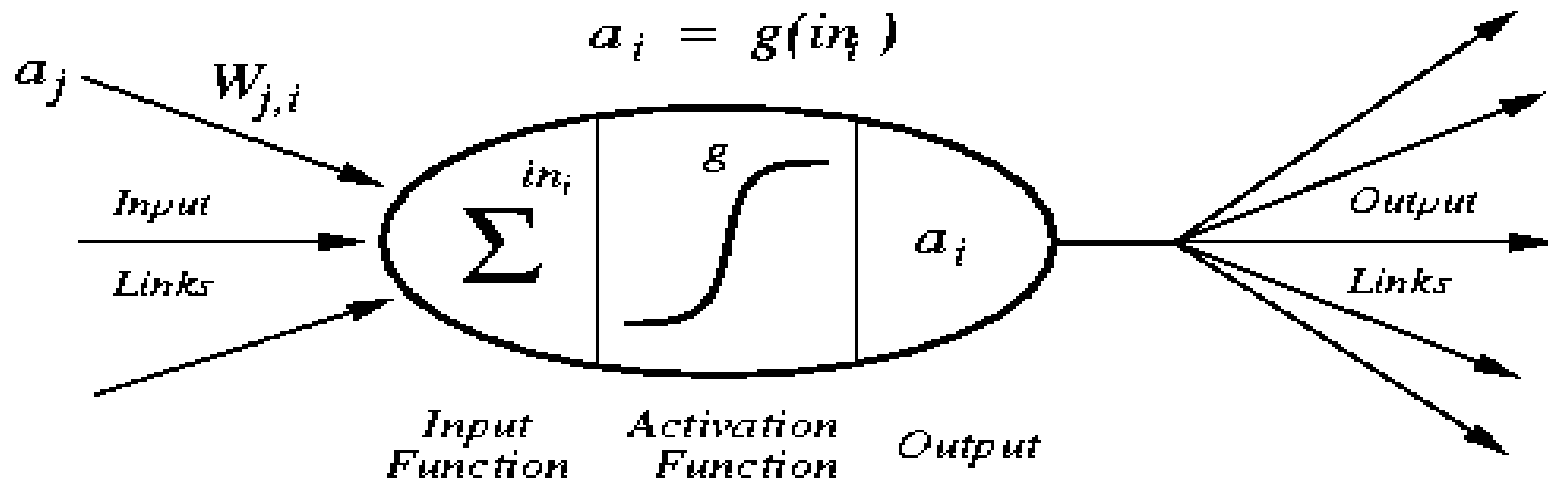
The First Neural Neural Networks

You can confirm that Y_2 works correctly

You can also check it works on the spreadsheet



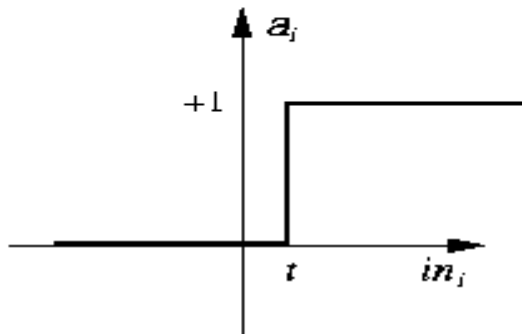
Modelling a Neuron



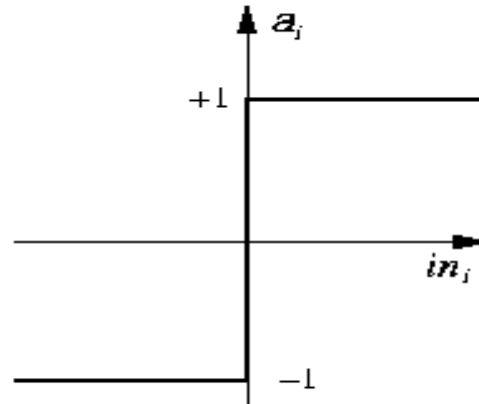
$$in_i = \sum_j W_{j,i} a_j$$

- a_j : Activation value of unit j
- $w_{j,i}$: Weight on the link from unit j to unit i
- in_i : Weighted sum of inputs to unit i
- a_i : Activation value of unit i
- g : Activation function

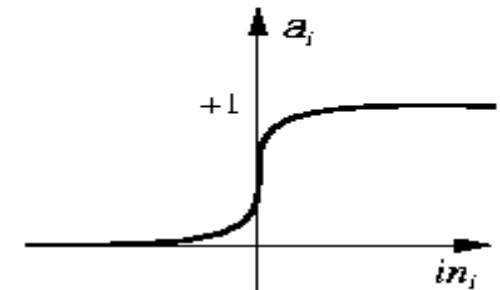
Activation Functions



(a) Step function



(b) Sign function



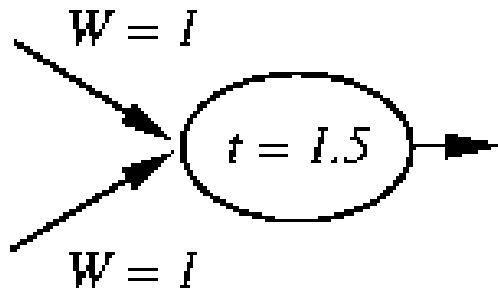
(c) Sigmoid function

- **Step_t(x) = 1 if x >= t, else 0**
- **Sign(x) = +1 if x >= 0, else -1**
- **Sigmoid(x) = 1/(1+e^{-x})**
- **Identity Function**

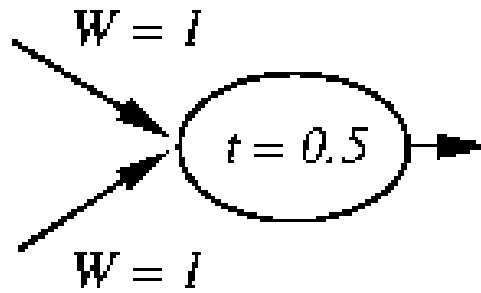
Simple Networks

	AND				OR				NOT	
Input 1	0	0	1	1	0	0	1	1	0	1
Input 2	0	1	0	1	0	1	0	1		
Output	0	0	0	1	0	1	1	1	1	0

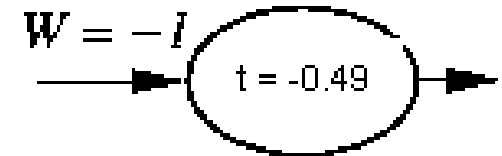
Simple Networks



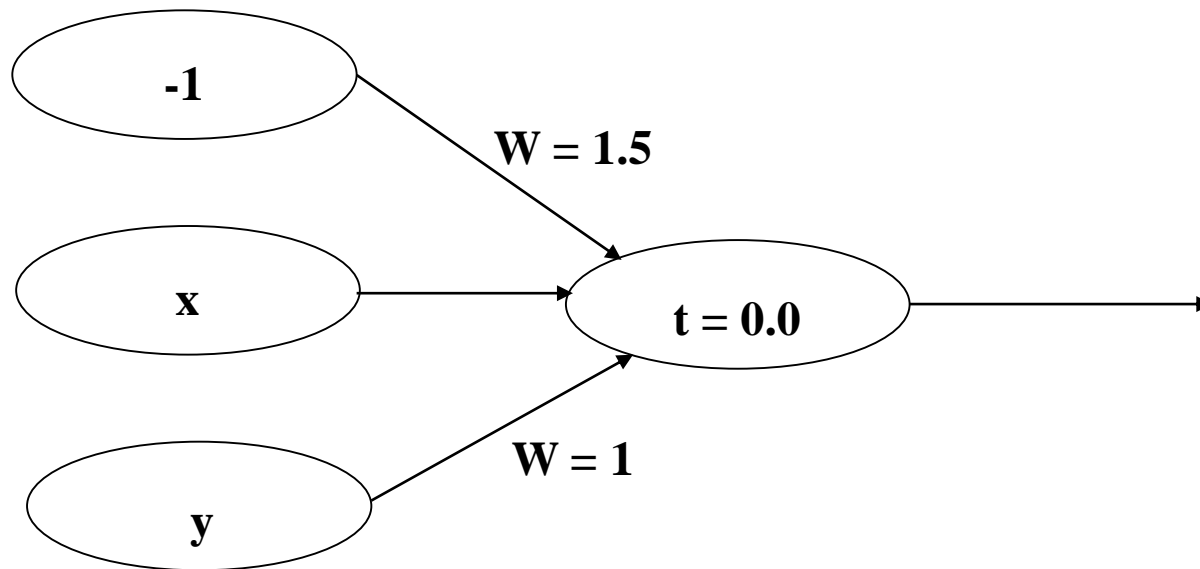
AND



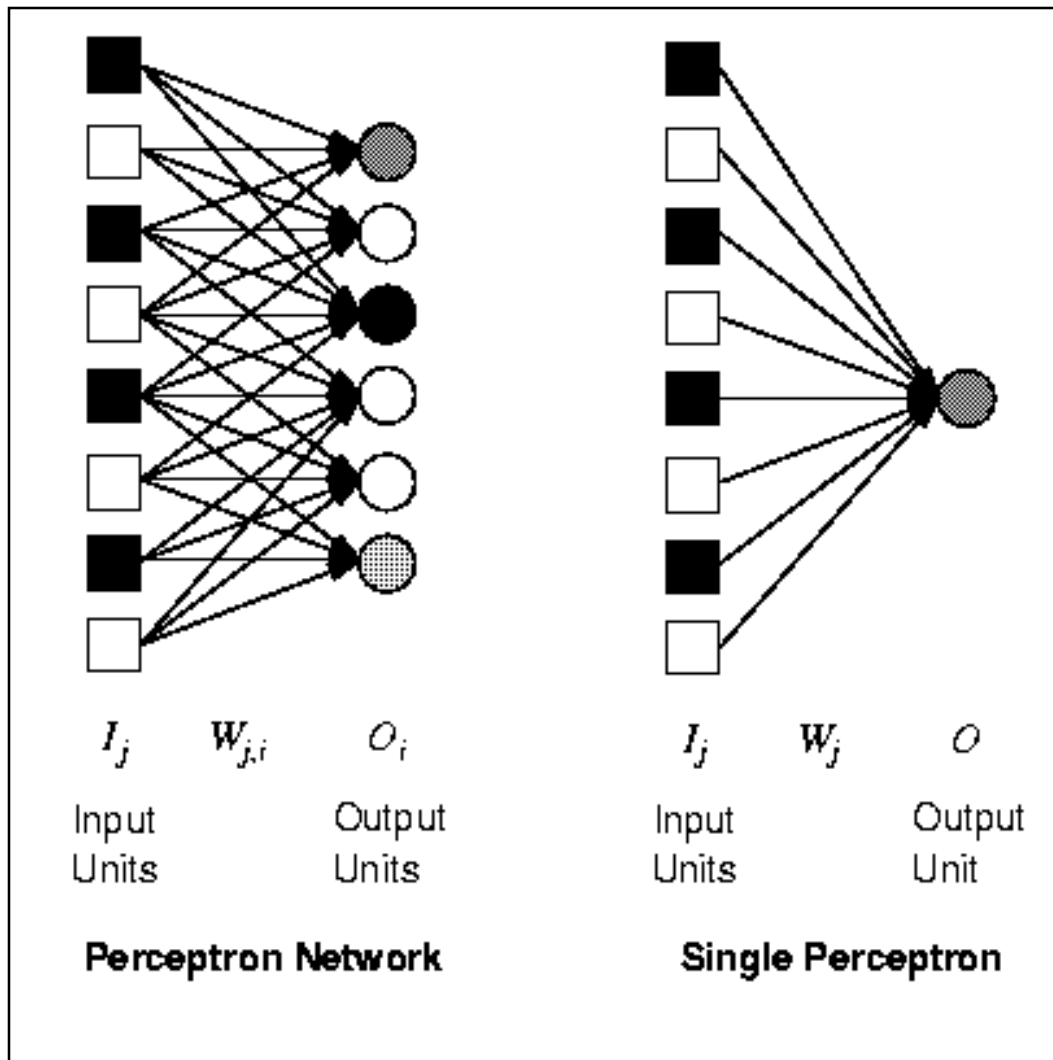
OR



NOT

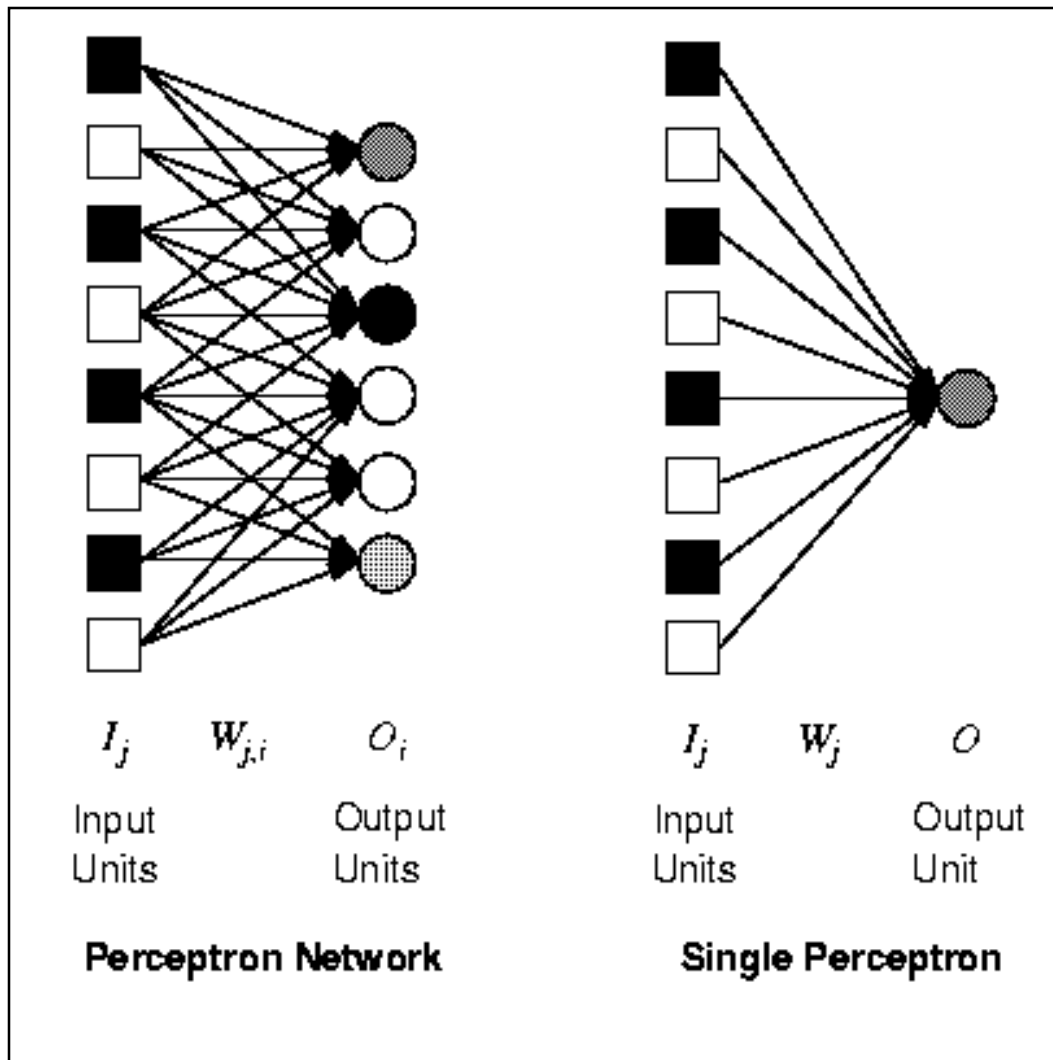


Perceptron



- **Synonym for Single-Layer, Feed-Forward Network**
- **First Studied in the 50's**
- **Other networks were known about but the perceptron was the only one capable of learning and thus all research was concentrated in this area**

Perceptron



- A single weight only affects one output so we can restrict our investigations to a model as shown on the right
- Notation can be simpler, i.e.

$$O = \text{Step}_0 \sum_j W_j I_j$$

What can perceptrons represent?

Input 1

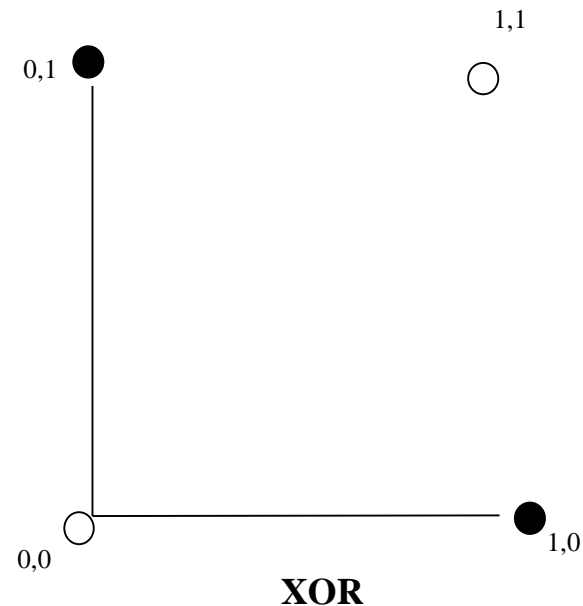
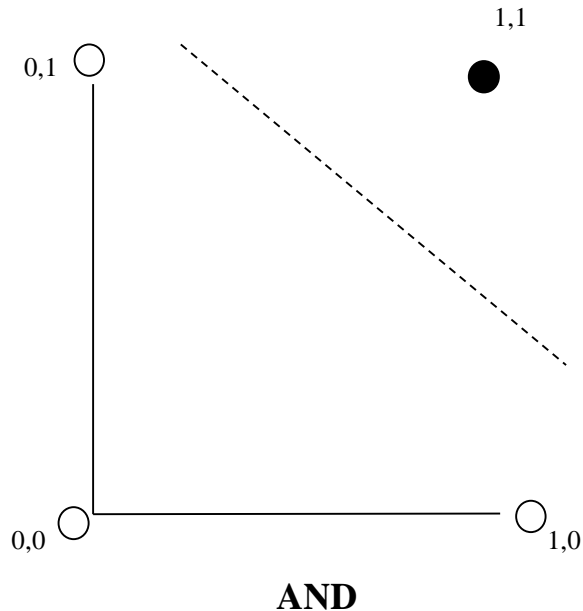
Input 2

Output

AND			
0	0	1	1
0	1	0	1
0	0	0	1

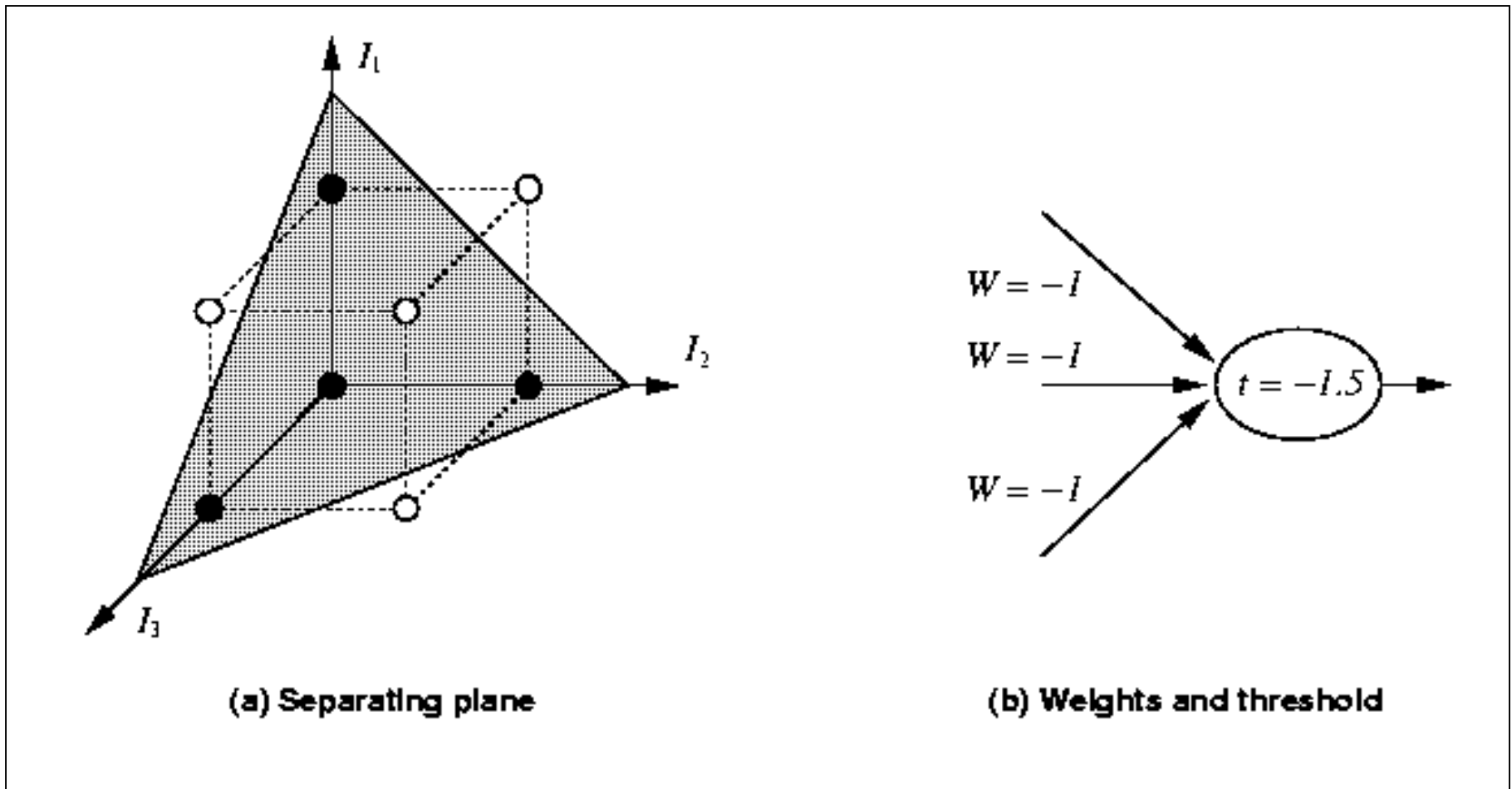
XOR			
0	0	1	1
0	1	0	1
0	1	1	0

What can perceptrons represent?



- **Functions which can be separated in this way are called *Linearly Separable***
- **Only linearly Separable functions can be represented by a perceptron**

What can perceptrons represent?



Linear Separability is also possible in more than 3 dimensions – but it is harder to visualise

Training a perceptron

Aim

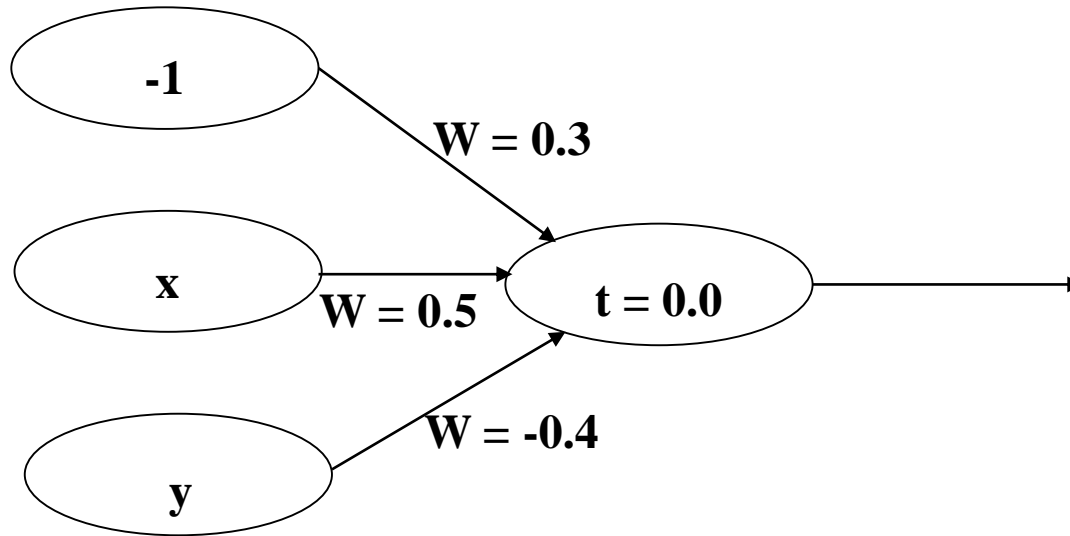
Input 1

Input 2

Output

AND			
0	0	1	1
0	1	0	1
0	0	0	1

Training a perceptrons



I_1	I_2	I_3	Summation	Output
-1	0	0	$(-1 * 0.3) + (0 * 0.5) + (0 * -0.4) = -0.3$	0
-1	0	1	$(-1 * 0.3) + (0 * 0.5) + (1 * -0.4) = -0.7$	0
-1	1	0	$(-1 * 0.3) + (1 * 0.5) + (0 * -0.4) = 0.2$	1
-1	1	1	$(-1 * 0.3) + (1 * 0.5) + (1 * -0.4) = -0.2$	0

Learning

While epoch produces an error

Present network with next inputs from epoch

$$\mathbf{Err} = \mathbf{T} - \mathbf{O}$$

If $\mathbf{Err} \neq 0$ then

$$\mathbf{W}_j = \mathbf{W}_j + \mathbf{LR} * \mathbf{I}_j * \mathbf{Err}$$

End If

End While

Learning

While epoch produces an error

Present network with next inputs from epoch

Err = T - O

If Err <> 0 then

$$W_j = W_j + LR * I_j * Err$$

End If

End While

Epoch : Presentation of the entire training set to the neural network.

In the case of the AND function an epoch consists of four sets of inputs being presented to the network (i.e. [0,0], [0,1], [1,0], [1,1])

Learning

While epoch produces an error

Present network with next inputs from epoch

Err = T - O

If Err <> 0 then

$$W_j = W_j + LR * I_j * Err$$

End If

End While

Training Value, T : When we are training a network we not only present it with the input but also with a value that we require the network to produce. For example, if we present the network with [1,1] for the AND function the training value will be 1

Learning

While epoch produces an error

Present network with next inputs from epoch

Err = T - O

If Err <> 0 then

$$W_j = W_j + LR * I_j * Err$$

End If

End While

Error, Err : The error value is the amount by which the value output by the network differs from the training value. For example, if we required the network to output 0 and it output a 1, then $Err = -1$

Learning

While epoch produces an error

Present network with next inputs from epoch

Err = T - O

If Err <> 0 then

$$W_j = W_j + LR * I_j * Err$$

End If

End While

Output from Neuron, O : The output value from the neuron

I_j : Inputs being presented to the neuron

W_j : Weight from input neuron (I_j) to the output neuron

LR : The learning rate. This dictates how quickly the network converges. It is set by a matter of experimentation. It is typically 0.1

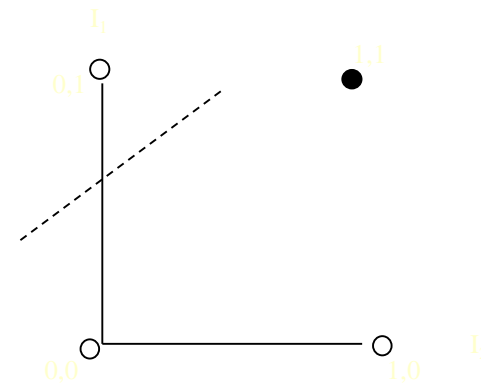
Learning

After First Epoch

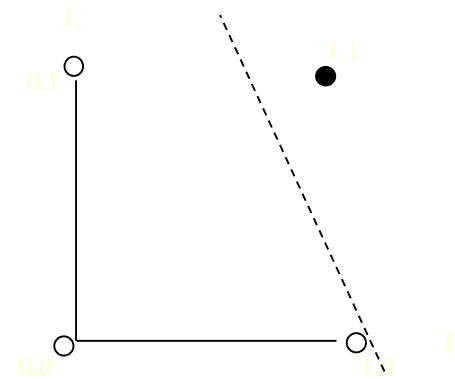
Note

I_1 point = W_0/W_1

I_2 point = W_0/W_2



At Convergence



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End of Neural Networks

